

UDC 535.327, 535.012

**THERMO-OPTIC PROPERTIES OF ORTHORHOMBIC BeAl<sub>6</sub>O<sub>10</sub> CRYSTAL**  
**Yumashev K.<sup>1</sup>, Malyarevich A.<sup>1</sup>, Vilejshikova E.<sup>1</sup>, Goman V.<sup>2</sup>, Pavlovski L.<sup>2</sup>**<sup>1</sup>Center for Optical Materials and Technologies of Belarusian National Technical University<sup>2</sup>Institute of Improvement of Professional Skills and Staff Retraining on New Directions of Engineering  
Technology and Economy of Belarusian National Technical University  
Minsk, Belarus

**Abstract.** Thermo-optic coefficients  $dn/dT$  were determined for orthorhombic BeAl<sub>6</sub>O<sub>10</sub> crystal for light polarizations  $E \parallel N_p$ ,  $N_m$  and  $N_g$  in the wavelength range of 0.4–1.1  $\mu\text{m}$ . Thermo-optic dispersion formulas for principal thermo-optic coefficients of BeAl<sub>6</sub>O<sub>10</sub> are presented for this spectral range. The principal  $dn/dT$  are positive and show a polarization-anisotropy:  $dn_p/dT = 6.4$ ,  $dn_m/dT = 5.0$ ,  $dn_g/dT = 5.6$  ( $10^{-6} \text{ K}^{-1}$ ) at wavelength of 0.83  $\mu\text{m}$ . Thermo-optic dispersion data are modeled in accordance with theory taking into account the contributions from the change of the electronic band gap with temperature and from the volumetric thermal expansion coefficient.

**Key words:** orthorhombic crystal, thermo-optic coefficient, BeAl<sub>6</sub>O<sub>10</sub> crystal, thermo-optic dispersion.

Correspondence address: Yumashev K.V., Nezavisimosti ave., 65/17, Minsk 220113, Republic of Belarus  
e-mail: kyumashev@bntu.by

**ТЕРМООПТИЧЕСКИЕ СВОЙСТВА ОРТОРХОМБИЧЕСКОГО КРИСТАЛЛА BeAl<sub>6</sub>O<sub>10</sub>**  
**Юмашев К.В.<sup>1</sup>, Маляревич А.М.<sup>1</sup>, Вилейшикова Е.В.<sup>1</sup>, Гоман В.И.<sup>2</sup>, Павловский Л.К.<sup>2</sup>**<sup>1</sup>Научно-исследовательский центр оптических материалов и технологий БНТУ<sup>2</sup>Институт повышения квалификации и переподготовки кадров по новым направлениям развития  
техники, технологии и экономики БНТУ  
Минск, Республика Беларусь

**Аннотация.** Определены термооптические коэффициенты  $dn/dT$  для орторомбического кристалла BeAl<sub>6</sub>O<sub>10</sub> для поляризаций света  $E \parallel N_p$ ,  $N_m$  и  $N_g$  в диапазоне длин волн 0,4–1,1 мкм. Для этого спектрального диапазона получены формулы дисперсии главных термооптических коэффициентов BeAl<sub>6</sub>O<sub>10</sub>. Значения  $dn/dT$  положительны и характеризуются поляризационной анизотропией:  $dn_p/dT = 6,4$ ,  $dn_m/dT = 5,0$ ,  $dn_g/dT = 5,6$  ( $10^{-6} \text{ K}^{-1}$ ) на длине волны 0,83 мкм. Данные по дисперсии термооптических коэффициентов моделируются в рамках модели, учитывающей вклады от изменения ширины электронной запрещенной зоны с температурой и от объемного коэффициента теплового расширения.

**Ключевые слова:** орторомбический кристалл, термооптический коэффициент, кристалл BeAl<sub>6</sub>O<sub>10</sub>, дисперсия термооптического коэффициента.

Адрес для переписки: Юмашев К.В., проспект Независимости, 65/17, Минск, 220113, Беларусь  
e-mail: kyumashev@bntu.by

Beryllium hexaaluminate BeAl<sub>6</sub>O<sub>10</sub> crystal is a promising laser matrix for various transition metal ions such as Cr<sup>3+</sup>, Ti<sup>3+</sup>, Ni<sup>2+</sup>. The BeAl<sub>6</sub>O<sub>10</sub>:Cr<sup>3+</sup> (Ti<sup>3+</sup>, Ni<sup>2+</sup>) crystals are promising for the use as active media for tunable solid state lasers in the spectral regions of 0.7–1.0  $\mu\text{m}$  (Cr<sup>3+</sup>), 0.6–1.1  $\mu\text{m}$  (Ti<sup>3+</sup>), and 1.35–1.65  $\mu\text{m}$  (Ni<sup>2+</sup>) [1]. The first laser operation for BeAl<sub>6</sub>O<sub>10</sub> crystal was achieved on Cr<sup>3+</sup> ions [2]. BeAl<sub>6</sub>O<sub>10</sub> crystals doped with Cr<sup>3+</sup> and Ti<sup>3+</sup> ions are promising media for the development of femto-second lasers [1]. However, thermo-optic properties of BeAl<sub>6</sub>O<sub>10</sub> (optically biaxial) crystal have not been studied in detail to date.

In the present work, we report on a measurements of the thermo-optic coefficients (TOCs,  $dn/dT$ ) of hexaaluminate crystal BeAl<sub>6</sub>O<sub>10</sub>.

Beryllium hexaaluminate BeAl<sub>6</sub>O<sub>10</sub> is grown by the Czochralski technique. The BeAl<sub>6</sub>O<sub>10</sub> is an orthorhombic crystal with space group *Pcam*, and thus is optically biaxial one. Optical properties of the BeAl<sub>6</sub>O<sub>10</sub> are described within the frame of the optical indicatrix with the orthogonal principal axes  $N_p$ ,  $N_m$ ,

and  $N_g$ . For BeAl<sub>6</sub>O<sub>10</sub>, these three axes are related to the crystallographic axes as follows:  $N_p // c$ ,  $N_m // a$  и  $N_g // b$  [3]. Like the three principal refractive indices, the BeAl<sub>6</sub>O<sub>10</sub> crystal should be characterized by three principal TOCs, namely  $dn_p/dT$ ,  $dn_m/dT$  and  $dn_g/dT$ .

To determine the TOCs, the sample from the BeAl<sub>6</sub>O<sub>10</sub> is prepared to be rectangular parallelepiped with dimensions 10×10×10mm<sup>3</sup>. The edges of the parallelepiped are parallel to the optical indicatrix (crystallographic) axes  $N_p(c)$ ,  $N_m(a)$ ,  $N_g(b)$ . All six surfaces of the sample were of a lasergrade quality.

For the determinations of the TOCs, the laser beam deviation technique for a material with a linear thermal gradient is used. Experimental setup and measurement procedure can be found elsewhere [4]. The measurements are performed at seven wavelengths by means of laser diodes (405 nm, 450 nm, 650 nm, and 800 nm), He-Ne laser (633 nm), and microchip diode-pumped Nd:YAG laser with frequency doubling (532 nm and 1064 nm). The laser beam deviation method allows one to measure the so-called thermal coefficients of the optical path

(TCOP),  $W=dn/dT+(n-1)\mu$ , where  $\mu$  is the linear thermal expansion coefficient in the direction of light propagation  $k$ ,  $n$  and  $dn/dT$  are the refractive index and TOC for corresponding light wavelength  $\lambda$  and polarization  $E$ . The precision of the TCOP measurements is  $\sim 10\%$ .

In order to extract the  $dn/dT$  value from the TCOP, literature data on the refractive index for  $BeAl_6O_{10}$  is used [3]. The principal linear thermal expansion coefficients  $\mu_{a(m)}$ ,  $\mu_{b(g)}$ , and  $\mu_{c(p)}$  are measured by means of Horizontal pushrod dilatometer Netzsch DIL 402 PC to be  $\mu_{a(m)} = 6.5$ ,  $\mu_{b(g)} = 6.9$ , and  $\mu_{c(p)} = 7.1$  ( $10^{-6} K^{-1}$ ). The value of  $\mu_{a(m)}$  obtained in present paper are in good accordance with the value of  $\mu_a = 6.8 \cdot 10^{-6} K^{-1}$  from [5].

For each light polarization  $E$ , two values of  $dn/dT$  are determined corresponding to two different directions of light propagation  $k$  by the formula  $dn_i/dT = W_{ij} - (n_i - 1) \mu_j$ , where  $i = p, m, g$  is the light polarization index,  $j = p, m, g$  is the index of the direction of light propagation, and  $i \neq j$ . Principal TOCs  $dn_p/dT$ ,  $dn_m/dT$ , and  $dn_g/dT$  are defined as the average over the corresponding values for the two directions of light propagation. The results are presented in the Table 1. All three principal TOCs for  $BeAl_6O_{10}$  are positive. For the whole studied spectral range, anisotropy of the TOCs characterized by  $dn_p/dT > dn_g/dT > dn_m/dT$ . The value of  $dn_{m(a)}/dT$  corresponds fairly well to the value of  $dn_a/dT = 11.6 \times 10^{-6} K^{-1}$  measured in [5] for visible spectral region with the minimum deviation method. There is no previous data on the  $dn_p/dT$  and  $dn_g/dT$ .

Table 1. Principal thermo-optic coefficients  $dn/dT$  ( $10^{-6} K^{-1}$ ) for  $BeAl_6O_{10}$

Wavelength, nm	$dn_p/dT$	$dn_m/dT$	$dn_g/dT$
405	15,6	11.9	13.6
450	13.0	9.5	10.8
532	9,7	7.9	8.9
633	7,9	6.25	6.85
650	7,7	6.0	6.55
800	6.55	5.0	5.5
1064	5.75	4.55	5.1

Experimental data on the wavelength dependence (dispersion) of the  $dn/dT$  are modeled by phenomenological model [6] according to which  $dn/dT$  is a sum of electronic and lattice contributions,  $dn/dT = (dn/dT)_e + (dn/dT)_L$ , where

$$(dn/dT)_e = (n^2_{\infty} - 1) / [2n(\lambda)] \{ -\mu_{vol} \lambda^2 / (\lambda^2 - \lambda_g^2) - (2/E_g) dE_g/dT [\lambda^2 / (\lambda^2 - \lambda_g^2)]^2 \}. \quad (1)$$

Here,  $n(\lambda)$  is the dispersion equation for refractive index,  $\lambda$  is the wavelength,  $n_{\infty}$  is the low frequency refractive index,  $\mu_{vol}$  is the volumetric thermal expansion coefficient,  $E_g$  is the electronic

bandgap,  $\lambda_g$  is the wavelength corresponding to  $E_g$ . For  $BeAl_6O_{10}$ , the lattice contribution  $(dn/dT)_L$  is small compared with the electronic part  $(dn/dT)_e$ , and can be neglected. Thus, the  $dn/dT$  values are considered to be  $dn/dT = (dn/dT)_e$ .

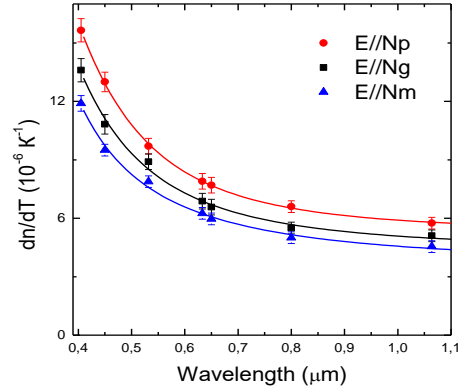


Figure 1 – Dispersion of principal thermo-optic coefficients  $dn/dT$  for  $BeAl_6O_{10}$  crystal: symbols – experimental data, lines – modeling using equation Eq. (1)

It follows from the Eq. (1) that the  $dn/dT$  value is controlled by two factors. The first factor  $(dn/dT)_\mu$  is the contribution from the volumetric thermal expansion coefficient and is negative because  $\mu_{vol}$  is normally positive for optical materials [6]. The second factor  $(dn/dT)_g$  is the contribution from the change of the electronic band gap with temperature and is normally positive because the value of  $dE_g/dT$  is normally negative for optical materials [6]. These two factors compete with one another giving positive or negative values of  $dn/dT$ .

The results of the TOCs dispersion simulation with Eq. (1) are presented in Fig. 1. The free fitting parameters are  $E_g$  and  $dE_g/dT$ . The best-fit parameters are 5.6 and  $-8.2$  (for  $E // N_p$ ), 6.0 and  $-8.2$  ( $E // N_m$ ), and 5.8 (eV) and  $-0.80$  ( $10^{-5} eV/K$ ) ( $E // N_g$ ), respectively. For  $BeAl_6O_{10}$ , the electronic bandgap was estimated to be 5.5 eV for unpolarized light propagating along  $N_p(c)$ -axis [3] which is in agreement with the data obtained in this work. According to the Eq. (1), the positive  $dn/dT$  coefficients of  $BeAl_6O_{10}$  are related to the weak thermal expansion, so that the contribution of the  $(dn/dT)_g$  term is dominant over the  $(dn/dT)_\mu$  one.

To calculate the  $dn/dT$  value at some arbitrary wavelength it is more convenient to use the analytical thermo-optic dispersion formulas which are obtained based on the principal thermo-optic coefficients given in Table 1. It is

$$dn_i/dT = A_i + B_i/\lambda^2 + C_i/\lambda^4 + D_i/\lambda^6 \quad (10^{-6} K^{-1}), \quad (2)$$

where  $i = p, m, g$ ,  $\lambda$  is in  $\mu m$ , and  $A, B, C, D$  are constant parameters chosen to give the best agreement with experimental TOCs data (Table 2).